# Properties of Phenylene-Based Hydrocarbon Bowls and Archimedene 

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Received: March 11, 2005; In Final Form: May 9, 2005


#### Abstract

Geometries, energies and magnetic shieldings are reported at the ab initio B3LYP/6-31G* level for the phenylene cluster $\mathrm{C}_{120}$ (archimedene) and eight phenylene-based hydrocarbon bowls consisting of four-, six-, and ten-membered rings. The six-membered rings are branched, angular, or terminal. The latter are the most aromatic, based upon NICS criteria and lack of substantial bond alternation. At the other extreme are branched rings, having less negative NICS values. Four-membered rings, except those on a rim, are nearly square. Regularities are found in the ab initio energies, heats of formation $\left(\Delta H_{\mathrm{f}}^{\circ}\right)$, and strain energies relative to those of hypothetical planar acyclic analogues. The bowls appear to have little aromatic character, and their interiors are but slightly shielded. Archimedene, with $\Delta H_{\mathrm{f}}^{\circ}=2191 \mathrm{kcal} / \mathrm{mol}$, has energetic and structural properties akin to those of phenylene-based bowls.


The past two decades have seen syntheses and studies of convex polyhedral clusters of carbon atoms based upon networks of fused five- and six-membered unsaturated rings: fullerenes and their bowl-shaped hydrocarbon fragments. An analogous class of bowls could be based upon phenylene units: alternately fused unsaturated four- and six-membered rings. $\mathrm{C}_{120}$, the polyhedral phenylene known as archimedene, ${ }^{1}$ with 20 sixmembered, 30 four-membered, and 12 ten-membered rings corresponds to fullerene $\mathrm{C}_{60}$, having 20 six-membered and 12 five-membered rings; both are of $I_{h}$ symmetry. Archimedene and its fragment hydrocarbons, primarily bowls, are the subject of this study. The bowls are of interest in their own right, and as synthetic intermediates in rational syntheses of archimedene. Phenylene-based bowls are also potential nanomaterials such as nanotips and semiconductors.

Synthetic realization and characterization of many acyclic phenylenes have come largely from the efforts of Vollhardt and collaborators, ${ }^{2}$ in a variety of motifs, most recently helical phenylenes. ${ }^{2 f, g}$ The experimental work to date has been accompanied and to some extent encouraged by theoretical work. ${ }^{3}$

In this work ab initio theory is used to obtain energies, geometries, and magnetic shieldings of archimedene (1) and eight bowl-shaped phenylene hydrocarbons ( $\mathbf{2}-\mathbf{9}$, Charts 1 and 2). ${ }^{4}$ The selected bowls have hexagons, decagons, or rectangles of carbon atoms as their bases, giving rise to molecules of $C_{3 v}$, $C_{5 v}$, and $C_{2 v}$ symmetry, respectively (Table 1). The rings are nearly planar, exactly so when required by symmetry, as in the case of a base ring or any ring in archimedene. We denote each symmetrically equivalent set of six-membered rings $6 \mathrm{~A}, 6 \mathrm{~B}$, ..., in order of increasing "distance" from the base. Similarly, $4 \mathrm{~A}, 4 \mathrm{~B}, \ldots$ and $10 \mathrm{~A}, 10 \mathrm{~B}, \ldots$ are sets of four-membered and ten-membered rings.

Nucleus-independent chemical shifts (NICS) introduced by Schleyer and co-workers ${ }^{5}$ are used to assess the extent of aromatic or antiaromatic character by computation of the magnetic shielding at points $1 \AA$ from the centroids of the rings, both inside and outside the bowl.

[^0]

Methods. Ab initio calculations were performed with Gaussian $98^{6}$ on servers of the Digital Alpha architecture. Geometries were obtained from calculations in the $6-31 \mathrm{G}^{*}$ basis $^{7}$ at the B3LYP density-functional ${ }^{8}$ level. Such calculations give bond lengths in good agreement with experimental X-ray values, where available; for example, the average deviation between experiment and theory for [8]heliphene is $0.004 \AA .{ }^{2 g}$ Proton and ${ }^{13} \mathrm{C}$ chemical shifts relative to TMS and NICS values were calculated at the B3LYP/6-31G* geometries using the GIAO method $^{9}$ at the HF/6-31G* level. Vibrational frequencies were calculated at the B3LYP/6-31G* level, except for $\mathrm{C}_{108} \mathrm{H}_{8}$, $\mathrm{C}_{114} \mathrm{H}_{6}$, and $\mathrm{C}_{120}$, where the B3LYP/6-31G level was used. All of the frequencies were found to be real, ranging from 20 to 40 $\mathrm{cm}^{-1}$ for the lowest of each bowl. The lowest frequency of $\mathrm{C}_{120}$ is $124 \mathrm{~cm}^{-1}\left(t_{2 u}\right)$. The ab initio energies are listed in Table 1.

## CHART 1



Supplemented by zero-point and thermal corrections, they are used to calculate standard enthalpies of formation.

Geometries. The six-membered rings in phenylene bowls are branched, angular, or terminal, having, respectively, three, two, and one fused four-membered rings ("cyclobutadienes") and, equivalently, zero, two, and four hydrogen atoms. The sixmembered rings of archimedene are branched. Angular sixmembered rings are found on the bowl rims, except for $\mathrm{C}_{60} \mathrm{H}_{20}$
(6); derived from $\mathrm{C}_{30} \mathrm{H}_{10}$ (9, cyclic [5]phenylene, ${ }^{3 \mathrm{~b}, \mathrm{~d}}$ shown below viewed along its $C_{5}$ axis, it is one of several possible bowls having terminal but no angular rings.

The six-membered rings of archimedene have (formal) single and double bonds of lengths (B3LYP/6-31G*) 1.479 and 1.364 A. Nearly identical lengths are found in the larger bowls. For branched rings $6 \mathrm{~A}, 6 \mathrm{~B}$, and 6 C of $\mathrm{C}_{108} \mathrm{H}_{8}$ (3) and $\mathrm{C}_{114} \mathrm{H}_{6}$ (2) the longest and shortest bond lengths are $1.479 \pm 0.001$ and

## CHART 2



TABLE 1: Symmetries, Energies and Dipole Moments of Phenylene Bowls and Archimedene

|  | unique <br> rings | total <br> rings $^{a}$ | energy, h | dipole <br> moment, $\mathrm{D}^{b}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathbf{1} \mathrm{C}_{120} \mathrm{H}_{0}\left(I_{4}\right)$ | $1,1,1$ | $30,20,12$ | -4570.96328 | 0.0 |
| $\mathbf{2} \mathrm{C}_{114} \mathrm{H}_{6}\left(C_{3 v}\right)$ | $6,5,3$ | $27,19,9$ | -4346.09865 | 3.7 |
| $\mathbf{3 ~ C}_{108} \mathrm{H}_{8}\left(C_{2 v}\right)$ | $8,6,3$ | $25,18,8$ | -4118.78033 | 5.3 |
| $\mathbf{4} \mathrm{C}_{90} \mathrm{H}_{10}\left(C_{5 v}\right)$ | $3,3,2$ | $20,15,6$ | -3434.36576 | 7.5 |
| $\mathbf{5} \mathrm{C}_{72} \mathrm{H}_{12}\left(C_{2 v}\right)$ | $5,4,2$ | $15,12,4$ | -2749.94619 | 7.5 |
| $\mathbf{6 ~ C}_{60} \mathrm{H}_{20}\left(C_{5 v}\right)$ | $2,2,1$ | $10,10,1$ | -2297.85495 | 4.3 |
| $\mathbf{7 ~ C}_{60} \mathrm{H}_{12}\left(C_{3 v}\right)$ | $3,3,1$ | $12,10,3$ | -2292.84782 | 6.9 |
| $\mathbf{8} \mathrm{C}_{48} \mathrm{H}_{12}\left(C_{2 v}\right)$ | $3,3,1$ | $9,8,2$ | -1835.75073 | 5.4 |
| $\mathbf{9}_{30} \mathrm{H}_{10}\left(C_{5 v}\right)$ | $1,1,1$ | $5,5,1$ | -1148.87380 | 3.2 |
| $\mathbf{1 0} \mathrm{C}_{60} \mathrm{H}_{20}\left(D_{5 d}\right)^{c}$ | $1,1,0$ | $10,10,0$ | -2297.76139 | 0.0 |

${ }^{a}$ Number of four-membered, six-membered, and ten-membered rings, respectively. ${ }^{b}$ The sense of the electric dipole is from the base toward the rim. ${ }^{c}$ Not a bowl, but a circular band of angular sixmembered rings.
$1.364 \pm 0.001$. Branched six-membered rings along rims show somewhat more bond alternation. Thus, ring 6D of $\mathrm{C}_{114} \mathrm{H}_{6}$ (2) and rings 6 D and 6 E of $\mathrm{C}_{108} \mathrm{H}_{8}(3)$ have the longest and shortest lengths of 1.486 and $1.358 \pm 0.001$.

Angular six-membered rings show less bond alternation than the branched rings. For ring 6 E of $\mathrm{C}_{114} \mathrm{H}_{6}(2), 6 \mathrm{~F}$ of $\mathrm{C}_{108} \mathrm{H}_{8}$ $(3)$, and 6 B of $\mathrm{C}_{90} \mathrm{H}_{10}(4)$ the bond lengths are $1.444 \pm 0.001$ and $1.367 \pm 0.001 \AA$. The five equivalent terminal sixmembered rings of $\mathrm{C}_{60} \mathrm{H}_{20}(6)$ show the least bond alternation: 1.424 and 1.379 . The fact that they are the most aromatic rings is confirmed by NICS(1) values.

The (planar) four-membered rings of archimedene are approximately square, with formal single $C C$ bonds endocyclic and exocyclic to the six-membered rings of lengths 1.479 and $1.477 \AA$, respectively. Four-membered rings of the phenylene bowls, excluding those lining the hydrogenated rim, are also nearly square: the shorter, $1.474 \pm 0.002$, and the longer, 1.480 $\pm 0.001$. Four-membered rings on a rim have bond lengths of up to $1.503 \AA$.

Energetics. Energies of phenylene bowls (Table 1) show regularities such as those found in the sequence $\mathrm{C}_{72} \mathrm{H}_{12}$ (5), $\mathrm{C}_{48} \mathrm{H}_{12}(8)$, and $\mathrm{C}_{60} \mathrm{H}_{12}(7)$. Thus, $\Delta E$ for reaction 1 is only $0.86 \mathrm{kcal} / \mathrm{mol}$, arising from ab initio energy and zero-point contributions of 0.80 and $0.06 \mathrm{kcal} / \mathrm{mol}$.

$$
\begin{equation*}
\mathrm{C}_{72} \mathrm{H}_{12}(\mathbf{5})+\mathrm{C}_{48} \mathrm{H}_{12}(\mathbf{8}) \rightarrow 2 \mathrm{C}_{60} \mathrm{H}_{12}(\mathbf{7}) \tag{1}
\end{equation*}
$$

Similarly, a small $\Delta E, 3.75 \mathrm{kcal} / \mathrm{mol}$, is found for reaction 2 , from ab initio energy and zero-point contributions of 4.15 and $-0.40 \mathrm{kcal} / \mathrm{mol}$.

$$
\begin{align*}
2 \mathrm{C}_{90} \mathrm{H}_{10}+5 \mathrm{C}_{48} \mathrm{H}_{12} & \rightarrow 2 \mathrm{C}_{30} \mathrm{H}_{10}+5 \mathrm{C}_{72} \mathrm{H}_{12} \\
2(\mathbf{4})+5(\mathbf{8}) & \rightarrow 2(\mathbf{9})+5(\mathbf{5}) \tag{2}
\end{align*}
$$

The small ab initio contributions depend upon equal numbers of six-membered rings of each type in products and reactants; for example, a total of 30 branched and 40 angular rings in reaction 2. Such ring-conserving reactions may be termed

TABLE 2: $\Delta H_{\mathrm{f}}^{\circ}$ and Extra Strain Energies, kcal/mol

|  | $\Delta H_{\mathrm{f}}^{\circ}{ }^{\circ}$ | $\Delta H_{\mathrm{f}}^{\circ}(\text { planar })^{b}$ | $\mathrm{ESE}^{c}$ |
| :--- | :---: | :---: | :---: |
| $\mathbf{1} \mathrm{C}_{120} \mathrm{H}_{0}\left(I_{h}\right)$ | 2191 | 1983 | 208 |
| $\mathbf{2} \mathrm{C}_{114} \mathrm{H}_{6}\left(C_{3 v}\right)$ | 1997 | 1808 | 189 |
| $\mathbf{3} \mathrm{C}_{108} \mathrm{H}_{8}\left(C_{2 v}\right)$ | 1858 | 1683 | 175 |
| $\mathbf{4} \mathrm{C}_{90} \mathrm{H}_{10}\left(C_{5 v}\right)$ | 1501 | 1361 | 140 |
| $\mathbf{5} \mathrm{C}_{72} \mathrm{H}_{12}\left(C_{2 v}\right)$ | 1145 | 1038 | 107 |
| $\mathbf{6} \mathrm{C}_{60} \mathrm{H}_{20}\left(C_{5 v}\right)$ | 781 | 747 | 34 |
| $\mathbf{7 \mathrm { C } _ { 6 0 } \mathrm { H } _ { 1 2 } ( C _ { 3 v } )}$ | 927 | 839 | 88 |
| $\mathbf{8} \mathrm{C}_{48} \mathrm{H}_{12}\left(C_{2 v}\right)$ | 708 | 641 | 67 |
| $\mathbf{9} \mathrm{C}_{30} \mathrm{H}_{10}\left(C_{5 v}\right)$ | 410 | 369 | 41 |
| $\mathbf{1 0} \mathrm{C}_{60} \mathrm{H}_{20}\left(D_{5 d}\right)$ | 812 | 738 | 74 |

${ }^{a}$ Calculated using homocyclic reactions with inclusion of zero-point energies and thermal effects. ${ }^{b}\left(\Delta H_{\mathrm{f}}^{\circ}\right)$ of a hypothetical planar acyclic phenylene having the same number of angular, branched, and terminal six-membered rings. Additive enthalpic increments $\mathrm{H}_{\mathrm{a}}, \mathrm{H}_{\mathrm{b}}$, and $\mathrm{H}_{\mathrm{t}}$ are given in the text. ${ }^{c}$ Extra strain energy attributable to nonplanarity.
"homocyclic." Small zero-point contributions are anticipated for any hydrocarbon reaction of zero molecularity, by an empirical formula. ${ }^{10}$

Enthalpies of formation ( $\mathrm{kcal} / \mathrm{mol}$ ) of phenylene bowls (Table 2) were obtained from homocyclic reactions involving the bowl of interest, $D_{2 h}$ biphenylene $\left(\mathrm{C}_{12} \mathrm{H}_{8}\right), C_{2 v}$ [3]phenylene $\left(\mathrm{C}_{18} \mathrm{H}_{10}\right)$, and branched $D_{3 h}$ [4]phenylene $\left(\mathrm{C}_{24} \mathrm{H}_{12}\right)$. Experimental values of $\Delta H_{\mathrm{f}}^{\circ}$ for the latter three are $100.5,{ }^{11 \mathrm{a}} 174.3,{ }^{11 \mathrm{~b}}$ and $249.9,{ }^{11 \mathrm{~b}}$ respectively. Thus, for $\mathrm{C}_{90} \mathrm{H}_{10}(\mathbf{4})$, use of reaction 3 and ab initio enthalpies corrected for zero-point energies and thermal effects leads to $\Delta H_{\mathrm{f}}^{\circ}=1501$.

$$
\begin{equation*}
5 \mathrm{C}_{18} \mathrm{H}_{10}+10 \mathrm{C}_{24} \mathrm{H}_{12} \rightarrow \mathrm{C}_{90} \mathrm{H}_{10}(4)+20 \mathrm{C}_{12} \mathrm{H}_{8} \tag{3}
\end{equation*}
$$

Reactions 4 and 5 furnish $\Delta H_{\mathrm{f}}^{\circ}=781$ and 2191 for $\mathrm{C}_{60} \mathrm{H}_{20}$ (6) and $\mathrm{C}_{120}(\mathbf{1})$, respectively.

$$
\begin{gather*}
5 \mathrm{C}_{24} \mathrm{H}_{12} \rightarrow 2 \mathrm{C}_{60} \mathrm{H}_{20}(\mathbf{6})+5 \mathrm{C}_{12} \mathrm{H}_{8}  \tag{4}\\
20 \mathrm{C}_{24} \mathrm{H}_{12} \rightarrow \mathrm{C}_{120}(\mathbf{1})+30 \mathrm{C}_{12} \mathrm{H}_{8} \tag{5}
\end{gather*}
$$

Magnetic Shielding. Chemical shifts of protons, which generally increase with size of the bowl, range from $\delta 6.4$ in $\mathrm{C}_{48} \mathrm{H}_{12}(\mathbf{8})$ to 7.2 in $\mathrm{C}_{114} \mathrm{H}_{6}(\mathbf{2})$; chemical shifts for the terminalring protons of $\mathrm{C}_{60} \mathrm{H}_{20}\left(C_{5 v}\right)$ are $\delta 7.2$ and 7.3. All of these values are slightly downfield from those calculated for large zigzag phenylenes: 6.5 for the angular and $7.0-7.2$ for the terminal protons. ${ }^{3 a}$
${ }^{13} \mathrm{C}$ chemical shifts of the basal carbons of $\mathrm{C}_{90} \mathrm{H}_{10}(4), \mathrm{C}_{108} \mathrm{H}_{8}$ (3), and $\mathrm{C}_{114} \mathrm{H}_{6}$ (2) are in the narrow range $\delta 142-143$ vs 141 for archimedene. Carbon atoms on the rims resonate from $\delta$ 138 to 153 . The larger values of $150-153$ are those of carbons in angular rings, adjacent to a CH moiety. Hydrogen-bearing carbon atoms have ${ }^{13} \mathrm{C}$ chemical shifts of $120-122$, similar to $\delta 120$ of planar zigzag phenylenes. ${ }^{3 \mathrm{a}}$

The aromatic character of individual rings can be assessed by calculations of $\operatorname{NICS}(1)$ and $\operatorname{NICS}(-1)$ values, at points 1 $\AA$ from the ring centroids, inside and outside the bowls, respectively (Table 3). NICS(1) values are all algebraically smaller than NICS $(-1)$, indicating greater shielding within the bowl. Most aromatic are the five terminal rings of $\mathrm{C}_{60} \mathrm{H}_{20}(6)$, with $\operatorname{NICS}(1)$ and $\operatorname{NICS}(-1)$ values of -9.5 and -9.4 ppm . Other hydrogen-bearing rings have $\mathrm{NICS}(1)$ ranging from -5.1 to -8.7 . NICS(1) values for the branched six-membered rings range from -1.3 to -5.6 . The branched rings are less aromatic than the hydrogen-bearing rings, as is found for large zigzag phenylenes. ${ }^{3 a}$

NICS(1) values for the four-membered rings are, with one exception, positive, as is usually the case in phenylenes. ${ }^{3 b}$ The

TABLE 3: $\operatorname{NICS}(1)$ and $\operatorname{NICS}(-1)^{a}$ Values (ppm) of Phenylene Bowls

|  | ring size |  |  |
| :---: | :---: | :---: | :---: |
|  | six | four | ten |
| $1 \mathrm{C}_{120}$ | A: $-1.9(-1.3)$ | A: 3.2(4.2) | A: $-0.2(-0.0)$ |
| $2 \mathrm{C}_{114} \mathrm{H}_{6}$ | A: $-2.4(-1.5)$ | A: 2.8(4.1) | A: $-0.8(-0.1)$ |
|  | B: $-2.6(-1.2)$ | B: 2.3(4.3) | B: $-1.8(-0.9)$ |
|  | C: $-3.2(-1.3)$ | C: 2.3(4.6) | C: $-1.7(-0.5)$ |
|  | D: $-2.6(-1.2)$ | D: 1.6(4.0) |  |
|  | E: $-7.0(-5.3)$ | E: 0.2(1.7) |  |
|  |  | F: 2.2(4.3) |  |
| $3 \mathrm{C}_{108} \mathrm{H}_{8}$ | A: $-2.8(-1.3)$ | A: 2.5(4.2) | A: $-1.0(-0.2)$ |
|  | B: $-3.2(-1.3)$ | B: 2.2(4.2) | B: $-1.9(-1.0)$ |
|  | C: $-3.9(-1.7)$ | C: 2.2(4.6) | C: $-2.0(-0.7)$ |
|  | D: $-2.8(-1.3)$ | D: 1.5(3.9) |  |
|  | E: $-1.3(-0.0)$ | E: 0.7(3.6) |  |
|  | F: $-7.8(-5.7)$ | F: 0.0(1.8) |  |
|  |  | G: 2.0(4.5) |  |
|  |  | H: 1.3(3.6) |  |
| $4 \mathrm{C}_{90} \mathrm{H}_{10}$ | A: $-4.0(-1.6)$ | A: 1.9(4.7) | A: $-1.4(-0.2)$ |
|  | B: $-1.6(-0.1)$ | B: 0.5(3.4) | B: $-2.4(-0.9)$ |
|  | C: $-8.7(-6.2)$ | C: 0.9(3.7) |  |
| $5 \mathrm{C}_{72} \mathrm{H}_{12}$ | A: $-4.9(-1.8)$ | A: $1.6(5.4)$ | A: $-2.5(-0.9)$ |
|  | B: $-2.0(-0.3)$ | B: 0.5(3.9) | B: $-2.6(-1.0)$ |
|  | C: $-8.4(-6.1)$ | C: 1.2(3.8) |  |
|  | D: $-6.8(-4.7)$ | D: 0.6(3.2) |  |
|  |  | E: 3.9(6.7) |  |
| $6 \mathrm{C}_{60} \mathrm{H}_{20}$ | A: $-3.8(-2.0)$ | A: $-1.1(1.9)$ | A: $-5.3(-3.5)$ |
|  | B: $-9.5(-9.4)$ | B: 4.0(5.0) |  |
| $7 \mathrm{C}_{60} \mathrm{H}_{12}$ | A: $-5.6(-2.2)$ | A: 0.6(4.3) | A: $-2.7(-1.0)$ |
|  | B: $-2.3(-0.4)$ | B: 0.8(3.3) |  |
|  | C: $-6.8(-4.6)$ | C: 4.0(6.7) |  |
| $8 \mathrm{C}_{48} \mathrm{H}_{12}$ | A: $-2.7(-0.7)$ | A: 0.1(3.6) | A: $-2.7(-1.0)$ |
|  | B: $-7.2(-5.0)$ | B: 1.1(3.8) |  |
|  | C: $-5.1(-3.2)$ | C: 3.2(5.9) |  |
| $9 \mathrm{C}_{30} \mathrm{H}_{10}$ | A: $-5.6(-3.8)$ | A: 3.2(5.6) | A: $-2.2(-0.6)$ |
| $10 \mathrm{C}_{60} \mathrm{H}_{20}$ | A: $-6.0(-4.0)$ | A: 1.6(4.2) |  |

${ }^{a} \operatorname{NICS}(-1)$ values are in parentheses. $\operatorname{NICS}(1)$ and $\operatorname{NICS}(-1)$ are isotropic shieldings $1 \AA$ from the ring centroid in a direction perpendicular to the mean plane of the ring and, respectively, inside and outside the bowl. For benzene, $\operatorname{NICS}(1)=-12.8$; for cyclobutadiene, $\operatorname{NICS}(1)=17.5$.
few examples of small negative $\operatorname{NICS}(1)$ values in fourmembered rings include those of the branched $D_{3 h}$ [4]phenylene. ${ }^{3 \mathrm{~b}}$ NICS values for the ten-membered rings are all small and negative, implying slight aromatic character, with the possible exception of $\mathrm{C}_{60} \mathrm{H}_{20}(6)$.

## Discussion

Electric dipole moments of phenylene bowls (Table 1) are oriented along the bowl axis with the positive end toward the rim. Similarly directed dipole moments are calculated for fullerene bowls, with magnitudes somewhat smaller than those of the analogous phenylene bowls (e.g., $\mathrm{C}_{36} \mathrm{H}_{12}, 4.6 \mathrm{D}^{12}$ vs $\mathrm{C}_{60} \mathrm{H}_{12}, 7,6.9 \mathrm{D}$ ) owing, in part, to the steepness of the latter.

The large extent of bond alternation in their six-membered rings, and the near thermoneutrality of reactions 1 and 2 imply little aromatic character in phenylene bowls. This conclusion would seem to hold also for archimedene. Its cyclohexatrienic six-membered rings have NICS(1) and NICS $(-1)$ of -1.9 and -1.3 . From the $\Delta H_{\mathrm{f}}^{\circ}$ values of Table $2, \Delta H^{\circ}$ of reactions 6 and 7 are 9 and $6 \mathrm{kcal} / \mathrm{mol}$, the smallness implying that in terms of energies archimedene is akin to bowl-shaped phenylenes.

$$
\begin{align*}
2 \mathrm{C}_{90} \mathrm{H}_{10}(\mathbf{4}) & \rightarrow 2 \mathrm{C}_{30} \mathrm{H}_{10}(\mathbf{9})+\mathrm{C}_{120}(\mathbf{1})  \tag{6}\\
5 \mathrm{C}_{72} \mathrm{H}_{12}(\mathbf{5}) & \rightarrow 5 \mathrm{C}_{48} \mathrm{H}_{12}(\mathbf{8})+\mathrm{C}_{120}(\mathbf{1}) \tag{7}
\end{align*}
$$

We can estimate the extra strain energy (ESE) of a bowl or archimedene over and above that of a hypothetical planar acyclic phenylene with the same numbers of angular (a), branched (b), and terminal (t) rings. The $\Delta H_{\mathrm{f}}^{\circ}$ (planar) values of Table 2 are obtained from additive enthalpic increments (in $\mathrm{kcal} / \mathrm{mol}$ ): $\mathrm{H}_{\mathrm{a}}$ $=73.80, \mathrm{H}_{\mathrm{b}}=99.15$ and $\mathrm{H}_{\mathrm{t}}=50.25$. These are derived from the three experimental $\Delta H_{\mathrm{f}}^{\circ}$ values ${ }^{11}$ of planar phenylenes; they are refinements of the values suggested previously. ${ }^{3 c}$ ESE values range from 34 for $\mathrm{C}_{60} \mathrm{H}_{20}(\mathbf{6})$ to $208 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{C}_{120}$ (1). They generally increase with molecular size, as do the values per carbon atom, all $<2.0$. This underscores, once again, the flexibility of phenylenes, whether planar, helical, ${ }^{3 a}$ or bowlshaped.

As noted previously, $\mathrm{C}_{60} \mathrm{H}_{20}(\mathbf{6})$ is obtained by appending a terminal ring to each of the five angular rings of $\mathrm{C}_{30} \mathrm{H}_{10}(\mathbf{9})$, a change adding little extra strain energy. Thus, the two compounds have similar ESE values: 34 versus $41 \mathrm{kcal} / \mathrm{mol}$, despite the fact that there are twice as many rings in $\mathbf{6}$ as in 9 . Conversely, archimedene fragment 10, a $D_{5 d}$ isomer of $\mathrm{C}_{60} \mathrm{H}_{20}$ (6) in the form of a circular band of 10 zigzag-arranged angular rings, has a higher ESE, $74 \mathrm{kcal} / \mathrm{mol}$.


10
An independent means of confirming the ESE values is available. B3LYP/6-31G* energies of planar, zigzag [19]- and [14]phenylene differ by -1148.93728 h , which is attributable to five angular six-membered rings. This value can serve as a reference energy for $\mathrm{C}_{30} \mathrm{H}_{10}(9)(-1148.87380 \mathrm{~h}$, Table 1), which itself is formed from five angular rings. The calculated strain energy, $40 \mathrm{kcal} / \mathrm{mol}$, compares favorably with $\mathrm{ESE}=41$ of Table 2.

Similarly, $D_{5 d} \mathrm{C}_{60} \mathrm{H}_{20}(\mathbf{1 0})$, composed of 10 angular sixmembered rings, is found to have a strain energy of $71 \mathrm{kcal} /$ mol from its ab initio energy (Table 1) plus $2 \times 1148.93728$. This is close to the ESE of 74 in Table 2. The strain energies calculated from "raw" ab initio values (Table 1) are not expected to be exactly the same as the ESE values of Table 2, which also contain zero-point and thermal energy corrections.

Regarding heats of formation, $\Delta H_{\mathrm{f}}^{\circ}=812$ for the $D_{5 d}$ isomer, as calculated from reaction 8.

$$
\begin{equation*}
10 \mathrm{C}_{18} \mathrm{H}_{10} \rightarrow \mathrm{C}_{60} \mathrm{H}_{20}(\mathbf{1 0})+10 \mathrm{C}_{12} \mathrm{H}_{8} \tag{8}
\end{equation*}
$$

This value is close to 820 , twice the value for $\mathrm{C}_{30} \mathrm{H}_{10}(\mathbf{9})$, two of which also contain 10 angular rings. The smaller $\Delta H_{\mathrm{f}}^{\circ}=$ 781 of the $C_{5 v}$ isomer 6 is attributable to its less strained, more aromatic terminal rings.
$D_{5 d} \mathrm{C}_{60} \mathrm{H}_{20}$ plays a role in homocyclic reaction 9a, the reactants and products of which each contain 20 branched and 10 angular six-membered rings, and 30 four-membered rings.

From the $\Delta H_{\mathrm{f}}^{\circ}$ values of Table 2, this reaction is thermoneutral ( $\Delta H^{\circ}=0$ ).

$$
\begin{equation*}
\mathrm{C}_{72} \mathrm{H}_{12}+\mathrm{C}_{108} \mathrm{H}_{8} \rightarrow \mathrm{C}_{60} \mathrm{H}_{20}\left(D_{5 d}\right)+\mathrm{C}_{120} \tag{9a}
\end{equation*}
$$

In contrast is the significant exothermicity of reaction $9 \mathrm{~b}, \Delta H^{\circ}$ $=-31 \mathrm{kcal} / \mathrm{mol}$, which arises from the imbalance of angular and terminal rings, that is, reaction $9 b$ is not homocyclic.

$$
\begin{equation*}
\mathrm{C}_{72} \mathrm{H}_{12}+\mathrm{C}_{108} \mathrm{H}_{8} \rightarrow \mathrm{C}_{60} \mathrm{H}_{20}\left(C_{5 v}\right)+\mathrm{C}_{120} \tag{9b}
\end{equation*}
$$

There is a series of relationships among the $\Delta H_{\mathrm{f}}^{\circ}$ values of Table 2. Archimedene can be prepared by hypothetically "splicing" $\mathrm{C}_{108} \mathrm{H}_{8}(3)$ and biphenylene, $\mathrm{C}_{12} \mathrm{H}_{8}$, extruding 16 hydrogen atoms (as $8 \mathrm{H}_{2}$ ) to form the requisite four additional four-membered rings (Table 1), with four angular and two terminal six-membered rings becoming six branched rings in the process. The enthalpy change of this splice is estimated to be $\Delta H_{\mathrm{f}}^{\circ}(\mathbf{3})+\Delta H_{\mathrm{f}}^{\circ}($ biphenylene $)+6 \mathrm{H}_{\mathrm{b}}-4 \mathrm{H}_{\mathrm{a}}-2 \mathrm{H}_{\mathrm{t}}$ or 1858 $+100.5+6 \times 99.15-4 \times 73.80-2 \times 50.25=2158 \mathrm{kcal} /$ mol. This value is only slightly smaller than $\Delta H_{\mathrm{f}}^{\circ}=2191$ for $\mathrm{C}_{120}(\mathbf{1})$, as would be expected for H -increments pertaining to planar rather than bent moieties.

Another such splice forms archimedene from two $\mathrm{C}_{60} \mathrm{H}_{12}$ (7) bowls. In this instance, six additional four-membered rings are formed and 12 angular six-membered rings become 12 branched rings. Its enthalpic change, $2 \times 927+12 \times(99.15-73.80)$ $=2158 \mathrm{kcal} / \mathrm{mol}$, again somewhat smaller than 2191. Archimedene may be formed by joining other members of Table 2, including two $\mathrm{C}_{60} \mathrm{H}_{20}\left(\mathbf{6}, C_{5 v}\right) ; \mathrm{C}_{90} \mathrm{H}_{10}$ (4) with $\mathrm{C}_{30} \mathrm{H}_{10}(\mathbf{9})$; $\mathrm{C}_{72} \mathrm{H}_{12}$ (5) with $\mathrm{C}_{48} \mathrm{H}_{12}$ (8); and $\mathrm{C}_{60} \mathrm{H}_{20}$ (10, $D_{5 d}$ ) with two $\mathrm{C}_{30} \mathrm{H}_{10}(9)$, one above and one below (the first step forming $\mathrm{C}_{90} \mathrm{H}_{10}$ ). The $\Delta H_{\mathrm{f}}^{\circ}$ values of $\mathbf{1}$ thereby obtained are similarly smaller than those computed by means of homocyclic reaction 5.

Acknowledgment. We thank Mr. Jon Leong for his continued assistance and interest in this work.

## References and Notes

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